



## Third Semester B.E. Degree Examination, June/July 2019

### Engineering Mathematics – III

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

#### Module-1

1. a. Obtain the Fourier series for the function :

$$f(x) = \begin{cases} -\pi & \text{in } -\pi < x < 0 \\ x & \text{in } 0 < x < \pi \end{cases}$$

Hence deduce that  $\sum_{n=1}^{\infty} \frac{1}{(2n-1)^2} = \frac{\pi^2}{8}$ .

(08 Marks)

- b. Express y as a Fourier series up to the second harmonics, given :

x	0	$\frac{\pi}{3}$	$\frac{2\pi}{3}$	$\pi$	$\frac{4\pi}{3}$	$\frac{5\pi}{3}$	$2\pi$
y	1.98	1.30	1.05	1.30	-0.88	-0.25	1.98

(08 Marks)

OR

2. a. Obtain the Fourier series for the function  $f(x) = 2x - x^2$  in  $0 \leq x \leq 2$ .

(08 Marks)

- b. Obtain the constant term and the first two coefficients in the only Fourier cosine series for given data :

x	0	1	2	3	4	5
y	4	8	15	7	6	2

(08 Marks)

#### Module-2

3. a. Find the Fourier transform of  $x e^{-|x|}$ .

(06 Marks)

- b. Find the Fourier sine transform of  $\frac{e^{-ax}}{x}$ ,  $a > 0$ .

(05 Marks)

- c. Obtain the z – transform of  $\sin n\theta$  and  $\cos n\theta$ .

(05 Marks)

OR

4. a. Find the inverse cosine transform of  $F(\alpha) = \begin{cases} 1-\alpha, & 0 \leq \alpha \leq 1 \\ 0, & \alpha > 1 \end{cases}$

Hence evaluate  $\int_0^{\infty} \frac{\sin 2t}{t^2} dt$ .

(06 Marks)

- b. Find inverse Z – transform of  $\frac{3z^2 + 2z}{(5z-1)(5z+2)}$

(05 Marks)

- c. Solve the difference equation  $y_{n+2} + 6y_{n+1} + 9y_n = 2^n$  with  $y_0 = 0, y_1 = 0$ , using z – transforms.

(05 Marks)

**Module-3**

- 5 a. Find the lines of regression and the coefficient of correlation for the data :

x	1	2	3	4	5	6	7
y	9	8	10	12	11	13	14

(06 Marks)

- b. Fit a second degree polynomial to the data :

x	0	1	2	3	4
y	1	1.8	4.3	2.5	6.3

(05 Marks)

- c. Find the real root of the equation  $x \sin x + \cos x = 0$  near  $x = \pi$ , by using Newton – Raphson method upto four decimal places.

(05 Marks)

**OR**

- 6 a. In a partially destroyed laboratory record, only the lines of regression of y on x and x on y are available as  $4x - 5y + 33 = 0$  and  $20x - 9y = 107$  respectively. Calculate  $\bar{x}, \bar{y}$  and the coefficient of correlation between x and y.

(06 Marks)

- b. Fit a curve of the type  $y = ae^{bx}$  to the data :

x	5	15	20	30	35	40
y	10	14	25	40	50	62

(05 Marks)

- c. Solve  $\cos x = 3x - 1$  by using Regula – Falsi method correct upto three decimal places, (Carryout two approximations).

(05 Marks)

**Module-4**

- 7 a. Give  $f(40) = 184$ ,  $f(50) = 204$ ,  $f(60) = 226$ ,  $f(70) = 250$ ,  $f(80) = 276$ ,  $f(90) = 304$ . Find  $f(38)$  using Newton's forward interpolation formula.

(06 Marks)

- b. Find the interpolating polynomial for the data :

x	0	1	2	5
y	2	3	12	147

By using Lagrange's interpolating formula.

(05 Marks)

- c. Use Simpson's  $\frac{3}{8}$ th rule to evaluate  $\int_0^{0.3} (1 - 8x^3)^{\frac{1}{2}} dx$  considering 3 equal intervals.

(05 Marks)

**OR**

- 8 a. The area of a circle (A) corresponding to diameter (D) is given below :

D	80	85	90	95	100
A	5026	5674	6362	7088	7854

Find the area corresponding to diameter 105, using an appropriate interpolation formula.

(06 Marks)

- b. Given the values :

x	5	7	11	13	17
f(x)	150	392	1452	2366	5202

Evaluate f(9) using Newton's divided difference formula.

(05 Marks)

- c. Evaluate  $\int_0^1 \frac{x}{1+x^2} dx$  by Weddle's rule taking seven ordinates.

(05 Marks)



### Module-5

- 9 a. Using Green's theorem, evaluate  $\int_C (2x^2 - y^2)dx + (x^2 + y^2)dy$  where C is the triangle formed by the lines  $x = 0$ ,  $y = 0$  and  $x + y = 1$ . (06 Marks)

- b. Verify Stoke's theorem for  $\vec{f} = (2x - y)i - yz^2j - y^2zk$  for the upper half of the sphere  $x^2 + y^2 + z^2 = 1$ . (05 Marks)

- c. Find the extremal of the functional  $\int_{x_1}^{x_2} \left\{ y^2 + (y')^2 + 2ye^x \right\} dx$ . (05 Marks)

**OR**

- 10 a. Using Gauss divergence theorem, evaluate  $\int_S \vec{f} \cdot \hat{n} ds$ , where  $\vec{f} = 4xz i - y^2 j + yzk$  and s is the surface of the cube bounded by  $x = 0, x = 1, y = 0, y = 1, z = 0, z = 1$ . (05 Marks)

- b. A heavy cable hangs freely under the gravity between two fixed points. Show that the shape of the cable is a Catenary. (06 Marks)

- c. Find the extremal of the functional  $\int_0^{\pi/2} \left\{ (y')^2 - y^2 + 4y \cos x \right\} dx$ , give that  $y = 0 = y(\pi/2)$ . (05 Marks)

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